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# Threshold Voltage and I-V Characteristics of AlGaAs/GaAs MODFETs

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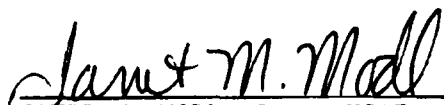
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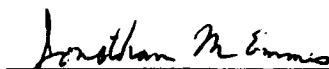
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<p>A strong inversion model, in the depletion layer approximation, of the I-V characteristics for MODFETs has been developed. The model describes MODFET I-V characteristics from subthreshold through saturation, over nine orders of magnitude in current. The saturation current is calculated and used to derive the experimental threshold voltage, which is determined by extrapolation of the saturation current (or square root of the current) vs gate voltage to zero current. It is shown that, for certain regions of acceptor doping, the experimentally determined threshold voltage can differ appreciably from the strong inversion definition. We show that this discrepancy is due to the effect of the depletion layer charge in the saturation region. Inclusion of the depletion layer charge in the analysis accounts for this difference and the difference between the saturation device capacitance per unit area and the AlGaAs layer capacitance per unit area.</p>					
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## I. INTRODUCTION

The dependence of the threshold voltage and radiation response of n-channel AlGaAs/GaAs modulation doped field-effect transistors (MODFETs) on acceptor doping density has been analyzed previously (Refs. 1 and 2). These analyses have been extended to describe the dependence of MODFET I-V characteristics on acceptor doping density. A triangular-well, one-subband, depletion layer model has been developed that applies over the range of I-V characteristics from subthreshold to saturation, some nine orders of magnitude in drain-source current.

For typical unintentional acceptor doping densities of  $10^{13}$  to  $10^{15} \text{ cm}^{-3}$ , characteristic in molecular beam epitaxy (MBE) grown structures, we show that the experimentally derived threshold voltage differs from the strong inversion model threshold voltage (Ref. 1) by 0.25 V at acceptor densities of  $10^{13} \text{ cm}^{-3}$ . At acceptor densities of  $10^{15} \text{ cm}^{-3}$ , the difference between the strong inversion model and the experimental extrapolation for the threshold voltage is about 0.12 V.

Inclusion of the acceptor doping density is shown to account for the discrepancy between the AlGaAs layer and the device capacitance per unit area described in the literature (Ref. 3).

## II. MODEL

The band structure of a typical AlGaAs(n)/GaAs heterojunction with a Schottky barrier,  $\phi_m$ , at the gate and a spacer layer at the interface under bias,  $V_g$ , is shown in Fig. 1.

Under the restrictions imposed by the assumptions cited in the caption of Fig. 1, Poisson's equation may be integrated across the structure to yield the applied gate voltage as a function of device geometry, doping densities, and channel charge,  $n_s$ :

$$V_g = V_0 + f(n_s) \quad (1)$$

where  $V_0$  is the difference between the Schottky barrier height and the sum of the AlGaAs/GaAs band offset and potential drop across the doped AlGaAs layer resulting from the ionized donors. The function  $f(n_s)$  may be written as

$$f(n_s) = (q/\epsilon)(d + a)(N_a W + n_s) + C_0(N_a W + n_s)^{2/3} + (kT/q)\ln[\exp(n_s n_c) - 1] \quad (2)$$

where  $C_0$  is a function of the Planck constant, the carrier effective mass, the elemental charge, and the permittivity of AlGaAs and GaAs, all assumed to be equal.  $C_0$  is equal to  $\sim 1.7 \times 10^{-9} \text{ V-cm}^{4/3}$ . Similarly, the charge density  $n_c$  is a function of physical constants and the effective mass of the carriers and is equal to  $\sim 8.4 \times 10^{11} \text{ cm}^{-2}$ . In the next section, we will exploit the mathematical properties of the function  $f(n_s)$  to derive the electrical properties of these devices.

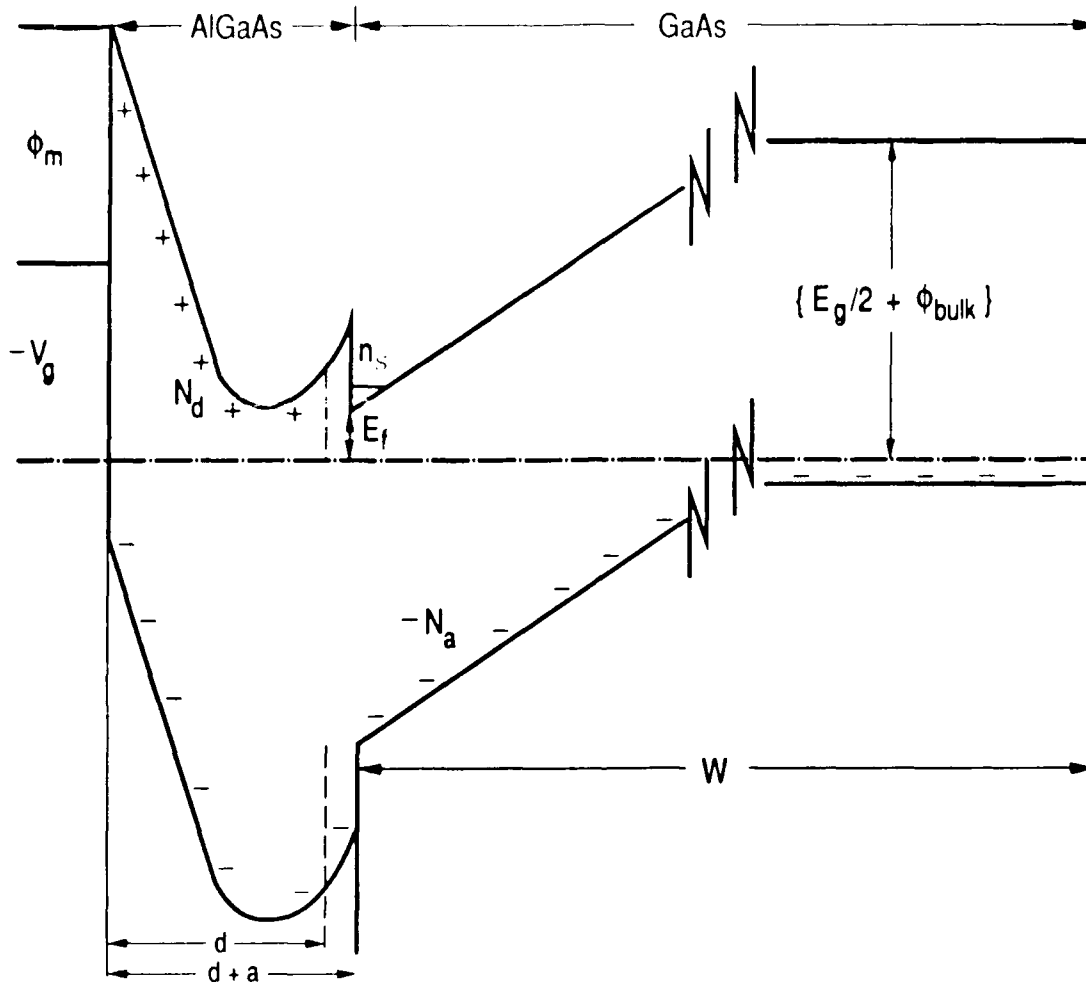


Fig. 1. Band Diagram of a Typical AlGaAs(n)/GaAs MODFET with Schottky Gate, Under Bias. In the depletion layer approximation, the donors and acceptors are assumed to be completely ionized in the doped AlGaAs layer,  $d$ , the spacer layer,  $a$ , and the depletion layer,  $W$ . The doping densities,  $N_d$  and  $N_a$ , are assumed to be constant. A delta-function channel charge distribution at the average channel width is assumed. Band bending from the interface at  $(d + a)$  to the edge of the depletion region  $(W + d + a)$  is the difference of position of conduction band relative to the Fermi level,  $E_g/2 + \phi_{\text{bulk}}$ , and the Fermi level relative to the bottom of the two-dimensional channel,  $E_f$ .



### III. ELECTRICAL PROPERTIES

#### A. THRESHOLD VOLTAGE

At threshold, we require that the channel density be equal to the acceptor density,  $N_a$ , times the average channel width,  $z_{av}$ , which may be calculated in the triangular-well approximation using variational wave functions (Ref. 4). This definition for threshold is consistent with the strong inversion definition of threshold in metal oxide semiconductor field effect transistors (MOSFETs). Our definition is the two-dimensional equivalent. Evaluating Eq. (2) at threshold and substituting into Eq. (1) yields the threshold voltage. The results of this calculation indicate that the threshold voltage is very sensitive to the acceptor doping density above  $\sim 10^{14} \text{ cm}^{-3}$ . The details of this calculation have been presented elsewhere (Ref. 1).

#### B. SUBTHRESHOLD I-V CHARACTERISTICS

In the subthreshold region, where  $n_s < N_a z_{av}$  over the whole channel,  $f(n_s)$  may be approximated as follows:

$$f(n_s) = (kT/q) \ln[g(n_s)] \quad (3)$$

Solving Eq. (3) for  $g(n_s)$ , expanding to first order about the threshold charge, and using Eq. (2) to determine the Taylor series expansion coefficients yield a convenient approximation for  $f(n_s)$  when substituted back into Eq. (3). Shown in Fig. 2 is the function  $f(n_s)$ , which is equivalent to  $(V_g - V_0)$  vs the log of the channel charge for two values of the acceptor doping density. The long dashes are the results of the approximation just described.

Using the subthreshold approximation for  $f(n_s)$  in Eq. (1), and solving for  $n_s$  in terms of  $V_g$ , we may calculate the subthreshold I-V characteristics using a charge control model (Ref. 5). The results of this calculation yield the MODFET equivalent of the MOSFET charge sheet subthreshold characteristics (Ref. 6). Details of these results will be discussed at the end of this

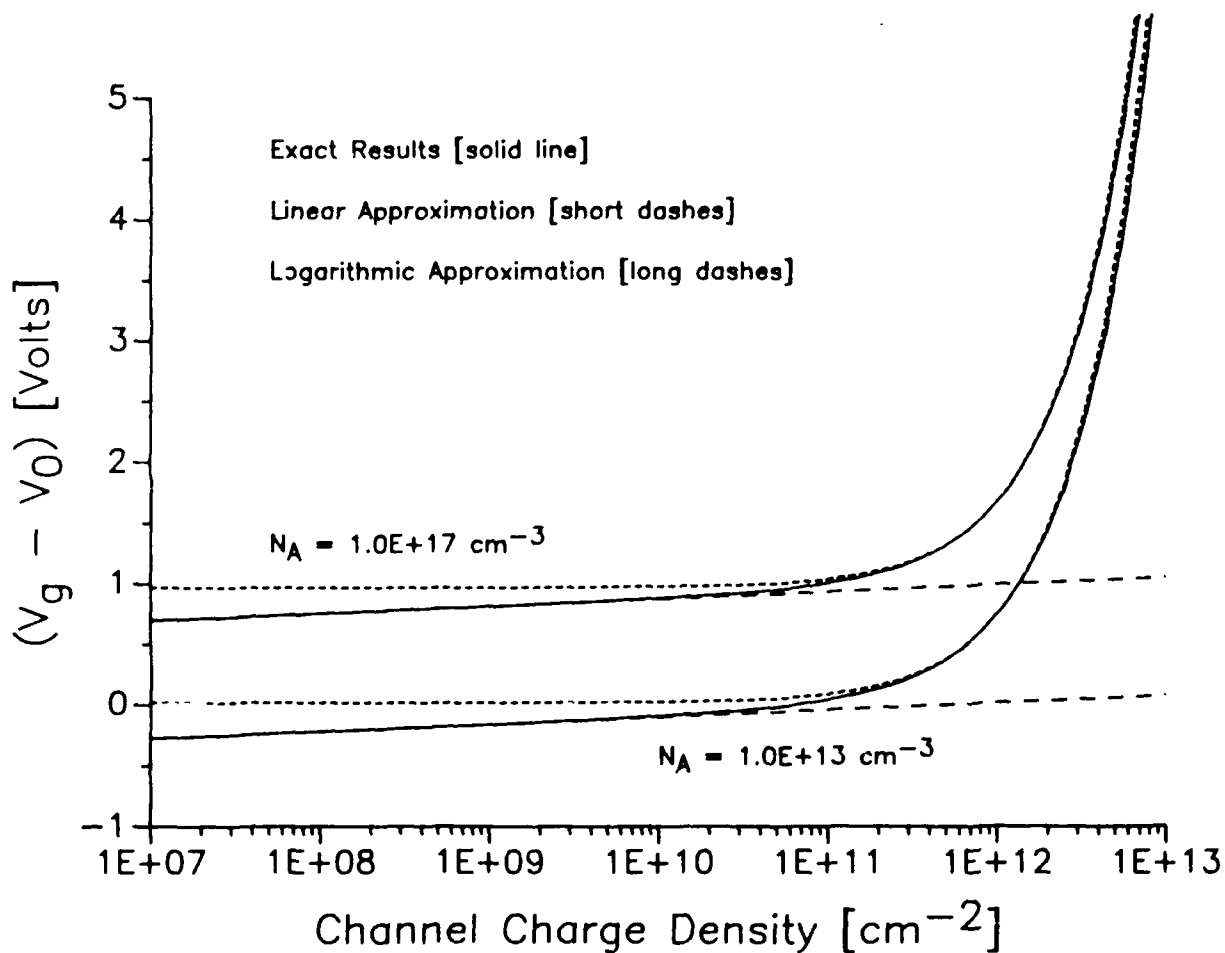


Fig. 2.  $V_g - V_0$  vs the Log of the Channel Charge. The solid lines are the results given by Eq. (2). The long dashes are the results of the Taylor expansion of  $f(n_s)$  in subthreshold, as described in the text. For an acceptor doping density of  $10^{13} \text{ cm}^{-3}$ , the threshold charge density is less than  $10^8 \text{ cm}^{-2}$ . Therefore, the subthreshold expansion is useful well above the threshold charge density. At an acceptor doping density of  $10^{17} \text{ cm}^{-3}$ , the threshold density is near  $10^{11} \text{ cm}^{-2}$ , and this expansion is only useful for channel charge densities below threshold. The short dashes are the results of a Taylor expansion of  $f(n_s)$  about  $n_c$ , as described in the text.

section in the context of the complete description of I-V characteristics from subthreshold to saturation.

### C. SATURATION I-V CHARACTERISTICS

We define the saturation region such that  $n_s \gg n_c$  over the whole channel. In this region, Eq. (2) may be expanded in a Taylor series in  $n_s$  about  $n_c$ . The results of this approximation to first order are shown as short dashes in Fig. 2. Above  $n_c$  ( $8.4 \times 10^{11} \text{ cm}^{-2}$ ), the expansion is quite good. Much below  $n_c$  ( $\sim 3 \times 10^{11} \text{ cm}^{-2}$ ), the first order expansion departs from the exact result and approaches a constant at low channel densities for all acceptor densities. As before, the approximation for  $f(n_s)$  may be substituted into Eq. (1), which is inverted to yield  $n_s$  as a function of  $V_g$ . The result is

$$n_s = n_c + K^{-1} [V_g - V_o - f(n_c)] / (kT/q) \quad (4)$$

where  $K$  is a constant that depends on the device geometry, doping densities, depletion width, and physical constants. This form for  $n_s$  is different than the form previously assumed (Ref. 5). The previous form ignores the contribution from  $n_c$  and  $f(n_c)$  and implicitly assumes that  $K^{-1}$  is  $(kT/q)C_{\text{A\&GaAs}}$ . The charge control model may then be used to calculate saturation I-V characteristics. We will defer the detailed discussion of these results to the end of this section.

### D. DEVICE CAPACITANCE

The device capacitance, when the charge density in the channel is greater than  $n_c$ , may be determined by differentiating Eq. (4) with respect to  $V_g$ . The resulting capacitance per unit area,  $C_{\text{area}}$ , may be cast in the following form (Ref. 3):

$$C_{\text{area}} = \epsilon / (d + a + \Delta d) \quad (5)$$

where  $\Delta d$  is given by

$$\Delta d = (2\epsilon/3q)C_o(N_a W + n_c)^{1/3} + 1.58(kT\epsilon/q^2)/n_c \quad (6)$$

When  $N_A W = n_c$ ,  $Ad$  is  $\sim 90$  Å. For large values of the acceptor doping density ( $\sim 10^{17}$  cm $^{-3}$ ),  $Ad$  is reduced to  $\sim 75$  Å. The constant  $K$ , in the previous subsection, is related to the capacitance per unit area as follows:

$$K^{-1} = (kT/q)C_{area} \quad (7)$$

#### E. EXPERIMENTAL THRESHOLD VOLTAGE

MOFET threshold voltages are determined experimentally by extrapolating the saturation current, or square root of the saturation current, vs gate voltage to zero. The gate voltage intercept is the experimentally determined threshold voltage. This is mathematically equivalent to solving Eq. (4) for the gate voltage when  $n_s$  is equal to zero. This calculation yields an experimental threshold voltage that differs from the strong inversion definition of the threshold voltage. The difference between the experimental value and the theoretical value is given by

$$V_{th} = f(n_c) - f(n_{th}) - qn_c C_{area} \quad (8)$$

where  $f(n_{th})$  is the value of Eq. (2) when evaluated at the threshold charge density. In Fig. 3, the threshold voltage difference is plotted vs the log of the acceptor density.

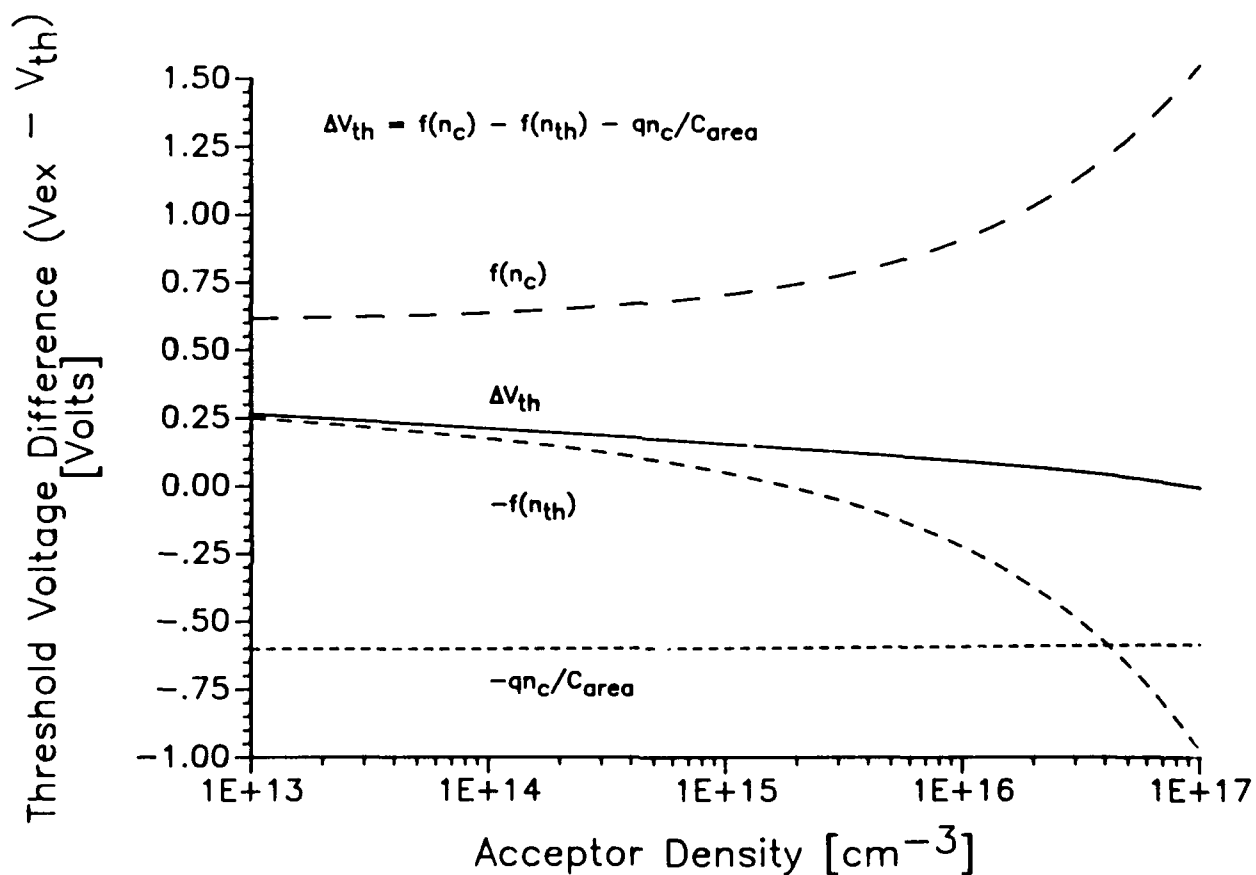


Fig. 3. Difference of the Experimental and the Strong Inversion Threshold Voltage vs the Log of the Acceptor Density. Each term in Eq. (8) is plotted separately. At low acceptor densities ( $< 10^{14} \text{ cm}^{-2}$ ), the difference may be as much as 0.25 V. This difference decreases as the acceptor density increases. Because this difference depends on the acceptor density, a comparison of experimental threshold voltages may not be appropriate if acceptor densities differ significantly.

#### IV. I-V CHARACTERISTICS FROM SUBTHRESHOLD TO SATURATION

In the charge control model, I-V characteristics are determined by substituting  $V_g - V_c(x)$  for  $V_g$  in Eq. (1), inverting the result to find  $n_s$  as a function of  $V_c(x)$ , substituting the result into the relationship for the current at position  $x$  in the channel, and integrating over the channel length (Ref. 5). In the subthreshold and saturation regions, as defined in subsections III.B and III.C, the approximations for  $f(n_s)$  permit a straightforward inversion of Eq. (1) for this purpose. As seen in Fig. 2, there is a region over which neither the subthreshold nor the saturation expansion applies. Because the integration for the current is performed over the voltage in the channel as well as over the channel length, an approximation must be determined that is continuous in the voltage, may be inverted to explicitly determine the channel charge in terms of the channel voltage, and reasonably approximates  $f(n_s)$  over the region.

To satisfy these requirements, we have derived a piecewise approximation for  $f(n_s)$  over this region. From the threshold charge to the channel charge,  $n_0$ , at which the exact  $f(n_s)$  is halfway between the subthreshold approximation at threshold and the saturation approximation at  $n_c$ , we have approximated  $f(n_s)$  as the log of a linear function of  $n_s$ . The two expansion coefficients are chosen so that this approximation for  $f(n_s)$  is exact at  $n_0$  and connects with the subthreshold approximation at the threshold channel density. From  $n_0$  to  $n_c$ , we have assumed that  $f(n_s)$  is linear in  $n_s$ . The two expansion coefficients are determined so that the approximation in this region is exact at the extremes,  $n_0$  and  $n_c$ .

The charge control model may now be used to calculate the I-V characteristics. A complication arises in the application of the charge control model because, for various values of the applied gate and drain-source voltages, different regions of the channel may have charge densities that must be calculated by different approximations to  $f(n_s)$ . Therefore, the current equation must be integrated placewise, although never over more than four regions, as

our piecewise approximation for  $f(n_s)$  requires. Over a range of gate (or drain-source) voltages, 10 possible combinations of regions might occur. Shown in Fig. 4 is the drain-source current vs drain-source voltage, for the parameters given, for various gate voltages using the approximations just described.

In Fig. 5, we show the drain-source current vs applied gate voltage for three values of the acceptor density and two values of the drain-source voltage.

Intrinsic transconductances may be calculated by differentiating the drain-source current relationships with respect to the gate voltage. Having done this calculation, we obtain transconductances of  $\sim 300 \text{ mS/mm}$  for structures with acceptor doping of  $10^{15} \text{ cm}^{-3}$ , evaluated at zero gate voltage and 2.5 V drain-source voltage.

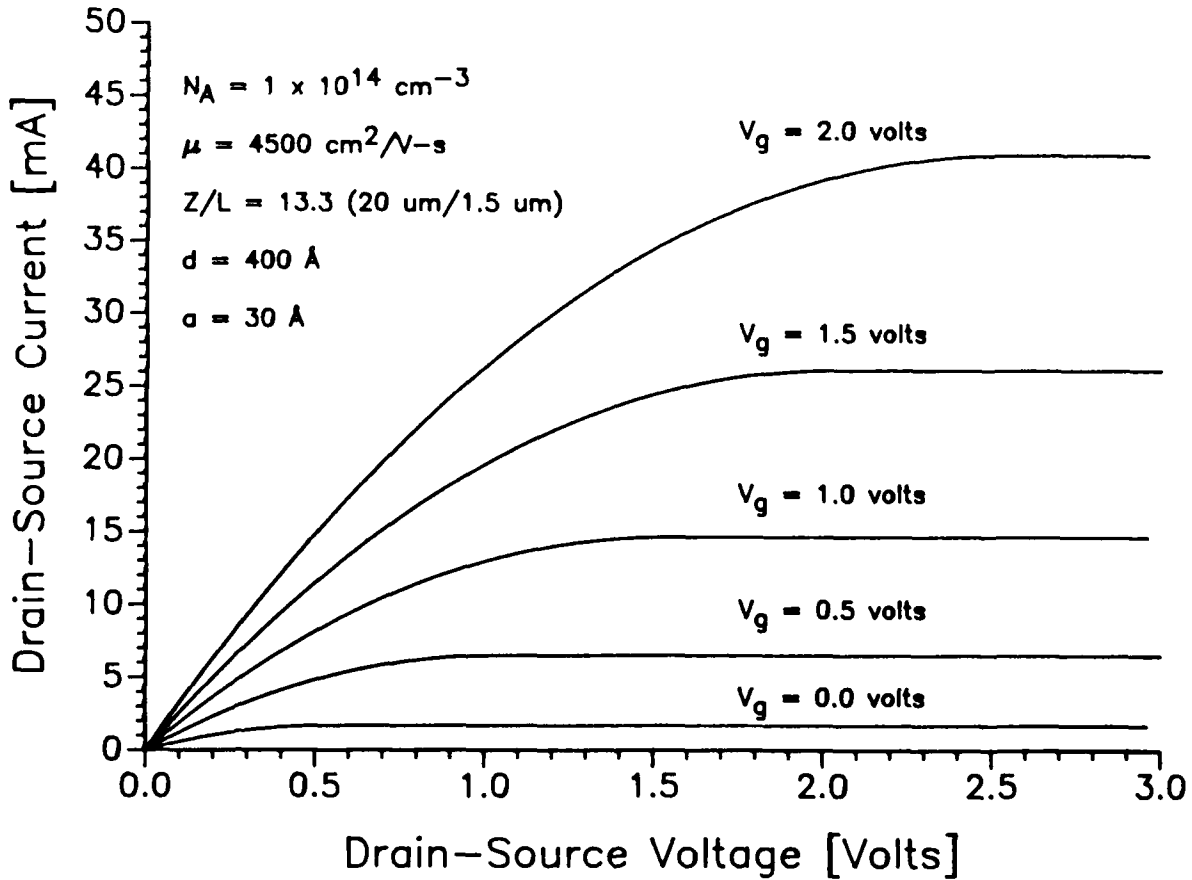


Fig. 4. Drain-Source Current vs Drain-Source Voltage. The current saturates at large drain-source voltage without velocity saturation or cutoff of the model invoked. When the whole channel is forced into the subthreshold charge region, the current depends on a constant plus an exponential in  $-V_{ds}$  which is negligible at large drain-source voltages.



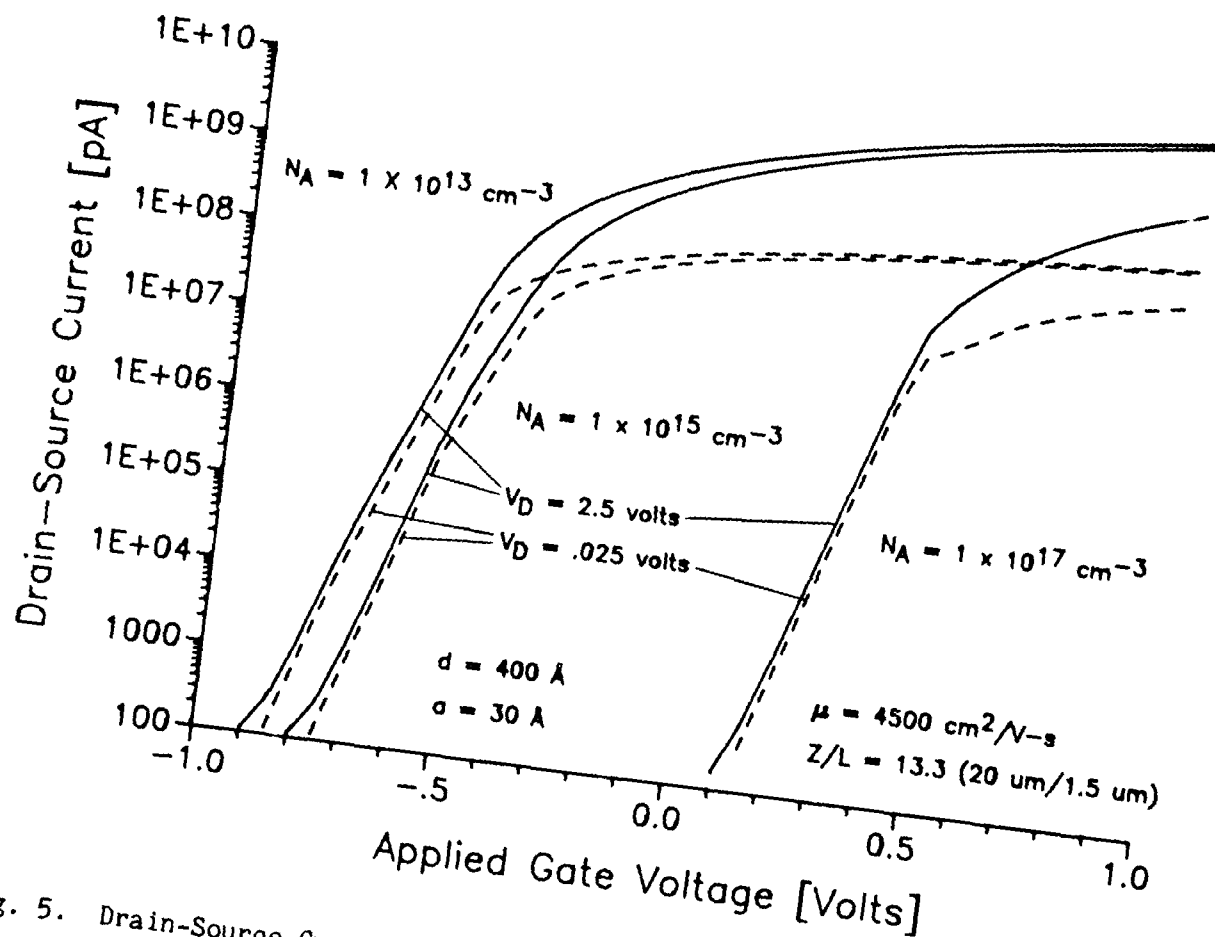


Fig. 5. Drain-Source Current vs Applied Gate Voltage. Current varies smoothly over nine orders of magnitude for all parameters except the highest acceptor density and smallest drain-source voltage. At high acceptor densities and low drain-source voltages, the approximations for  $f(n_s)$  at the threshold charge density have significantly different slopes, resulting in a kink in the dashed curve at 0.5 V.

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